Neutrinos from the Sun: Experimental results confronted with solar models

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(Received 27 May 1994)

For standard neutrinos, recent solar neutrino results together with the assumption of a nuclear powered Sun imply severe constraints on the individual components of the total neutrino flux: $\Phi_{\text{Be}} \leq 0.7 \times 10^9 \text{ cm}^{-2} \text{ s}^{-1}$, $\Phi_{\text{CNO}} \leq 0.6 \times 10^9 \text{ cm}^{-2} \text{ s}^{-1}$, and $64 \times 10^9 \text{ cm}^{-2} \text{ s}^{-1} \leq \Phi_{pp+pep} \leq 65 \times 10^9 \text{ cm}^{-2} \text{ s}^{-1}$ (at 1σ level). The bound on Φ_{Be} is in strong disagreement with the standard solar model (SSM) prediction $\Phi_{\text{Be}}^{\text{SSM}} \approx 5 \times 10^9 \text{ cm}^{-2} \text{ s}^{-1}$. We study a large variety of nonstandard solar models with low inner temperature, finding that the temperature profiles T(m) follow the homology relationship $T(m) = kT^{\text{SSM}}(m)$, so that they are specified just by the central temperature T_c . There is no value of T_c which can account for all the available experimental results. Even if we only consider the gallium and Kamiokande results, they remain incompatible. Lowering the cross section $p + {}^7\text{Be} \to \gamma + {}^8\text{B}$ is not a remedy. The shift of the nuclear fusion chain towards the pp-I termination could be induced by a hypothetical low energy resonance in the ${}^3\text{He} + {}^3\text{He}$ reaction. This mechanism gives a somehow better, but still bad, fit to the combined experimental data. We also discuss what can be learned from new generation experiments, planned for the detection of monochromatic solar neutrinos, about the properties of neutrinos and of the Sun.

PACS number(s): 96.60.Kx

I. INTRODUCTION

The aim of this paper is to examine whether there is still room for an astrophysics and/or nuclear physics solution of the solar neutrino problem, in the light of the most recent results of the gallium experiments [1,2].

We shall demonstrate that these results, when combined with the information arising from the chlorine [3] and Kamiokande [4] experiments and, most importantly, with the assumption of a nuclear powered Sun, severely constrain the individual components of the solar neutrino flux, under the hypothesis of standard (zero mass, no mixing, no magnetic moment,...) neutrinos.

The arguments leading to these constraints, already outlined in a previous paper [5], are essentially independent of solar models. The basic assumption concerning the Sun is that the *present* total neutrino flux can be derived from the *presently* observed value of the solar constant. We remark that these constraints have became much more stringent after the recent reports from GALLEX and SAGE [1,2].

For standard neutrinos, these results provide evidence that the nuclear energy production chain (see Fig. 1), is extremely shifted towards the pp-I termination and, as a consequence, the fluxes of $\nu_{\rm Be}$ and $\nu_{\rm CNO}$ are strongly reduced with respect to the predictions of standard solar models.

The situation is the following: (i) we can now compare theory and experiment at the level of individual fluxes; (ii) the solar neutrino problem, i.e., the discrepancy between experimental results and standard solar models, now affects also the ⁷Be-nuclei production, and not only the rare ⁸B neutrinos.

Next, we ask ourselves whether the solar neutrino problem is restricted to standard solar models. In this spirit, we analyze several nonstandard solar models with an enhanced *pp*-I termination. The main inputs of any solar model are listed in Table I. We are aware of just

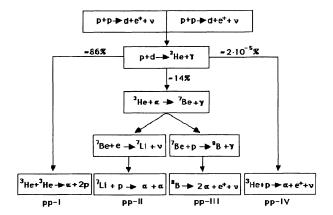


FIG. 1. The pp chain.

TABLE I. The main parameters P of solar models and their estimated relative uncertainties at 1σ level, $(\delta^P/P)^{\rm SSM}$ (here as in the text $\delta^P \equiv \delta P$). All values are as in Ref. [24], apart for S_{pp} , which is taken from the more recent Ref. [25]. Concerning solar age we refer to common wisdom, see Ref. [26]. In the last column we show, for the first four parameters, the values of $\zeta \equiv P/P^{\rm SSM}$ needed to account for $T_c/T_c^{\rm SSM} = 0.94$, when each input parameter is varied separately. In the same column we also show, for S_{33} and S_{34} , the values needed to account for $\Phi_{\rm Be} = 0.3 \, \Phi_{\rm Be}^{\rm SSM}$ (again when each input parameter is varied separately).

P	$\left(\frac{\delta^P}{P}\right)^{SSM}$	$\zeta = \frac{P}{P^{ exttt{SSM}}}$
$\overline{S_{pp}}$ Opacity	1%	1.7
Opacity	2.5%	0.63
Z/X	6%	0.30
$egin{array}{c} { m Age} \\ { m S_{33}} \end{array}$	3%	0.23
S_{33}	6%	11.0
$S_{34} \ S_{17}$	3%	0.3
S_{17}	9%	_

two ways for enhancing the *pp*-I termination acting on these inputs: (i) adjusting the parameters which affect the inner solar temperature, so as to build low inner-temperature solar models; (ii) adjusting the ³He nuclear cross sections.

We note that the $p+{}^7\mathrm{Be} \to \gamma + {}^8\mathrm{B}$ cross section does not influence the pp-I branch.

As a relevant and common feature of all the low innertemperature models, we find a homology relation for the temperature profiles, $T(m) = kT^{\rm SSM}(m)$, where k depends on the input parameters, but it is independent of the mass coordinate m in the inner radiative zone (at least for $m = M/M_0 < 0.97$), and SSM refers here and in the following to standard solar models. In other words, our numerical experiments disclose that a variation of the solar temperature in the center implies a definite variation in the entire inner radiative zone.

A consequence of this finding is that the different components of the neutrino flux depend basically only on the central temperature, and are almost independent of how that temperature is achieved. This in turn implies that, when performing a χ^2 analysis of the experimental data compared to the prediction of nonstandard solar models, it is sufficient to parametrize these nonstandard solar models by the central temperature. In other words, varying independently all the solar model parameters that influence the temperature does not yield a better fit than just varying the central temperature.

It is well known that it is not possible to get a good temperature fit due to the "discrepancy" between the Kamiokande and chlorine results [6–8], but the following questions are, nonetheless, interesting: (i) How much does the fit improve if one excludes one of the experimental results? (ii) Does this fit improve if one lowers the $p + {}^{7}\text{Be} \rightarrow \gamma + {}^{8}\text{B}$ cross section, as suggested from the analysis of recent data on the Coulomb dissociation of ${}^{8}\text{B}$ [9,10]?

Another way to shift the nuclear fusion chain towards

the pp-I termination without altering the inner solar temperature can be found in the realm of nuclear physics. In the light of the new neutrino results, we discuss whether a hypothetical low energy resonance in the ³He + ³He reaction, firstly advocated by Fowler [11], analyzed in Ref. [6], and presently investigated experimentally at Laboratori Nazionali del Gran Sasso (LNGS) [12], can reconcile theory and experiments.

Several new-generation experiments are being planned for the detection of monochromatic solar neutrinos produced in electron capture ($^7\text{Be} + e^- \to ^7\text{Li} + \nu$) and in the pep $(p+e^- \to d+n)$ reactions [13–15]. Furthermore, Bahcall [16,17] pointed out that thermal effects on monochromatic neutrino lines can be used to infer inner solar temperatures. In relation to the foregoing analysis, we discuss what can be learned from such future measurements about the properties of neutrinos and of the Sun.

Hata et al. [18] and Berezinsky [19] have recently performed independent studies similar in spirit to ours, and reached many of the same conclusions.

Concerning the organization of the paper, the solar-model-independent constraints on neutrino fluxes are presented in Sec. II and compared with the results of standard solar models in Sec. III. Section IV is devoted to the analysis of nonstandard solar models with lower temperatures, which are compared with experimental data in Sec. V. In Sec. VI we discuss the chances of a low energy resonance in the 3 He + 3 He channel, and in Sec. VII we remark on the relevance of future detection of the pep and 7 Be neutrinos. Our conclusions are summarized in the final section.

II. (ALMOST) SOLAR-MODEL-INDEPENDENT CONSTRAINTS ON NEUTRINO FLUXES

In this section we briefly update the constraints on neutrino fluxes derived in Ref. [5], in the light of the recent reports from GALLEX and SAGE [1,2]. While we refer to Ref. [5] for details, we recall here the main points.

(i) For standard neutrinos and under the assumption of a nuclear powered Sun, the components Φ_i of the total neutrino flux arriving onto the Earth are constrained by the equation of energy production

$$K = \sum_{i} \left(\frac{Q}{2} - \langle E \rangle_{i} \right) \Phi_{i}, \tag{1}$$

where K is the solar constant, Q is the energy released in the fusion reaction $4p + 2e \to \alpha + 2\nu$, and $\langle E \rangle_i$ is the average neutrino energy of the *i*th flux. In practice the relevant terms in Eq. (1) are just those corresponding to Φ_{pp+pep} , Φ_{Be} , and Φ_{CNO} .

(ii) In order to calculate $\langle E \rangle_i$, we take the ratio $\xi \equiv \Phi_{\rm pep}/\Phi_{pp+\rm pep}$ from the SSM ($\xi = 2.38 \times 10^{-3}$), and, similarly, the ratio $\xi \equiv \Phi_{\rm N}/\Phi_{\rm CNO} = 0.54$. Results are almost insensitive to these choices [5].

(iii) The signal S_X of the X experiment is represented

$$S_X = \sum_i X_i \Phi_i, \tag{2}$$

where the weighting factors X_i are cross sections for the ν detection reaction averaged over the (emission) spectrum of the *i*th component of the neutrino flux (note that the X_i are ordered according to the neutrino energy), and are shown in Table II.

(iv) We use the following experimental results, where systematic and statistical errors have been added in quadrature. For the gallium value, we use the weighted average of the GALLEX [1] and SAGE [2] results

$$S_{\rm Ga} = (78 \pm 10) \text{ SNU},$$
 (3)

where SNU denotes solar neutrino units. For the chlorine experiment we use the average of the 1970-1992 runs [3]:

$$S_{\rm Cl} = (2.32 \pm 0.26) \text{ SNU},$$
 (4a)

whereas the Kamiokande result reads

$$S_{\rm B}^{\rm Ka} = (2.9 \pm 0.42) \times 10^6 \,\,{\rm cm^{-2}\,s^{-1}}.$$
 (4b)

(v) We take the boron flux Φ_B , which enters in Eq. (2), from experiment. However, we can use *either* the Kamiokande result or the chlorine result (it is well known [6,7] that a choice between the two experiment is needed, otherwise one is forced to an unphysical value $\Phi_{Be} \leq 0$).

We have thus four unknowns Φ_{pp+pep} , Φ_{Be} , Φ_{CNO} , and Φ_{B} , which are constrained by the three equations (1), (3), and, alternatively, (4a) or (4b).

By exploiting the ordering properties of the X_i , as discussed in Ref. [5], and by using the new experimental results, one derives severe constraints, for standard neutrinos. As an example, by taking Φ_B from Kamioka,

TABLE II. For the *i*th component of the neutrino flux we show the average neutrino energy $\langle E \rangle$ and the averaged neutrino capture cross sections X_i (1 SNU cm² s = 10^{-36} cm²) for chlorine (Cl) and gallium (Ga), with errors at 1σ level. All data are from Ref. [22], but for the Cl cross section average over the ⁸B neutrino flux, which is taken from Ref. [27]. When averaging the pp and pep components we use the relative weights of our SSM (CDF94) (see Table III); similarly for ¹³N and ¹⁵O.

	$\langle E angle$	Cl	Ga
	[MeV]	$[10^{-9}\mathrm{SNU~cm^2s}]$	$[10^{-9}\mathrm{SNU~cm^2s}]$
pp	0.265	0.0	$1.18(1\pm0.02)$
pep	1.442	$1.6 \ (1 \pm 0.02)$	$21.5 \ (1 \pm 0.07)$
pp+pep	0.268		$1.23(1\pm0.02)$
⁷ Be	0.814	$0.24(1\pm0.02)$	$7.32(1\pm0.03)$
¹³ N	0.707	$0.17(1 \pm 0.02)$	$6.18(1\pm0.03)$
¹⁵ O	0.996	$0.68(1\pm0.02)$	$11.6 \ (1 \pm 0.06)$
CNO			
$(^{13}N + ^{15}O)$	0.840	$0.40(1\pm0.02)$	$8.67(1\pm0.05)$
⁸ B	6.71	1090.0 (1 ± 0.01)	2430.0 (1 ± 0.25)

for each assumption about Φ_{pp+pep} one has the minimum signal in GALLEX if all other neutrinos are from beryllium and the maximum signal if all other neutrinos are from CNO. By using similar procedures one finds the bounds depicted in Figs. 2–4. By conservatively using the chlorine result to determine the boron flux (this choice is the less restrictive on the fluxes), we find the following bounds on the fluxes, in units of 10^9 cm⁻² s⁻¹:

$$64 \leq \Phi_{pp+pep} \leq 65$$
 at 1σ ,
$$\Phi_{Be} \leq 0.7,$$

$$\Phi_{CNO} \leq 0.6,$$
 (5a)

and

$$61 \leq \Phi_{pp+pep} \leq 65$$
 at 3σ
$$\Phi_{Be} \leq 4.2,$$

$$\Phi_{CNO} \leq 3.6.$$
 (5b)

In summary, the gallium result together with the luminosity constraint implies that almost all neutrinos, if standard, come from the pp-I termination. The bounds of Eqs. (5) are very strict since even a small flux of other (and more energetic) than the pp neutrinos gives an ap-

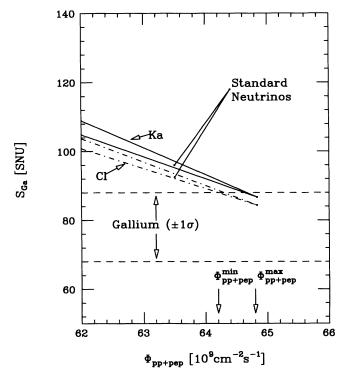


FIG. 2. The gallium signal $S_{\rm Ga}$ is shown as a function of the neutrino flux $\Phi_{pp+{\rm pep}}$. Standard neutrinos correspond to the area inside the solid (dot-dashed) lines if the Kamiokande (chlorine) value for the boron contribution is used. The gallium result $\pm 1\sigma$ is shown. The lower limit for the pp-I flux is thus $\Phi_{pp+{\rm pep}}^{\rm min} = 64.2 \times 10^9 \ {\rm cm}^{-2} \, {\rm s}^{-1}$ ($64.6 \times 10^9 \ {\rm cm}^{-2} \, {\rm s}^{-1}$). The upper limit $\Phi_{pp+{\rm pep}}^{\rm max} = 64.8 \times 10^9 \ {\rm cm}^{-2} \, {\rm s}^{-1}$ is given by the luminosity constraint.

preciable contribution to the gallium signal. This is why an experimental result with 10% accuracy can fix the Φ_{pp+pep} at the level of about 2%.

We note that the bounds have become much more stringent than those reported in Ref. [5], because both the central value and the error of the gallium result have decreased, so that now the experimental result is even closer to the minimal signal which is obtained when all neutrinos come from the pp-I termination ($\Phi_{pp+pep} = 65 \times 10^9 \text{ cm}^{-2} \text{ s}^{-1}$).

Concerning the assumptions leading to Eqs. (5), we remark that the main hypothesis is that the present Sun is nuclear powered [see Eq. (1)], whereas the values chosen for ξ and η are unessential (see again Ref. [5]).

III. STANDARD SOLAR MODELS AND EXPERIMENTAL DATA

The relevance of the bounds derived in the preceding section can be best illustrated by comparing them with the results of standard solar model computations. For a few representative calculations we present the main input parameters of these models in Table III, and the resulting neutrino fluxes in Table IV.

Let us remark that we can now compare not only the total signals predicted by the theory and measured by experiments, but also several individual fluxes, as shown in Table IV. In particular, we find that the upper limit for $\Phi_{\rm Be}$, implied by the experiment at the 1σ level, is 7 times smaller than $\Phi_{\rm Be}^{\rm SSM}$, whereas, at the same level of accuracy, $\Phi_{\rm B}$ is about a factor of 2 smaller with respect to the SSM (in Table IV the experimental upper bound on $\Phi_{\rm B}$ is obtained from the less constraining result, i.e., the Kamiokande value). A suppression of $\Phi_{\rm Be}$ stronger than $\Phi_{\rm B}$ was already implied by the comparison between Kamiokande and chlorine results, while we derived it using essentially only the gallium experiments.

In addition, we remind that the theoretical calculation for Φ_B is the most questionable of the flux calculations, due to the well known uncertainties. In our opinion, the discrepancy between theory and experiment for the ⁷Be flux is much more serious than the one for the ⁸B flux. In other words, it seems to us that the solar neutrino

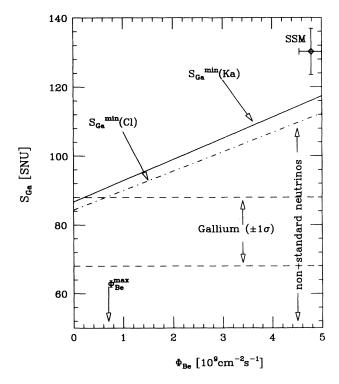


FIG. 3. The gallium signal $S_{\rm Ga}$ is shown as a function of the neutrino flux $\Phi_{\rm Be}$. The gallium result $\pm 1\sigma$ is shown (dashed lines). For standard neutrinos, the allowed region is above the straight line $S_{\rm Ga}^{\rm min}$. The region consistent with the gallium result and standard neutrinos is the shaded area. The allowed flux has to be smaller than $\Phi_{\rm Be}=7\times 10^8~{\rm cm}^{-2}~{\rm s}^{-1}$ ($2\times 10^8~{\rm cm}^{-2}~{\rm s}^{-1}$) at 1σ , if the boron contribution is derived from chlorine (Kamiokande) experiment. The result of our SSM is also shown (\Diamond).

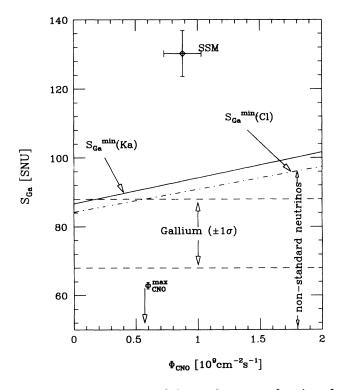


FIG. 4. The gallium signal $S_{\rm Ga}$ is shown as a function of the neutrino flux $\Phi_{\rm CNO}$. The gallium result $\pm 1\sigma$ is shown (dashed lines). For standard neutrinos, the allowed region is above the straight line $S_{\rm Ga}^{\rm min}$. The region consistent with the gallium result and standard neutrinos is the shaded area. The allowed flux has to be smaller than $\Phi_{\rm CNO}=6\times 10^8 {\rm cm}^{-2} {\rm s}^{-1}$ ($2\times 10^8 {\rm cm}^{-2} {\rm s}^{-1}$) at 1σ , if the boron contribution is derived from chlorine (Kamiokande) experiment. The result of our SSM is also shown (\Diamond).

problem is now at the level of the branching between the pp-I and pp-II terminations.

In order to reconcile the theoretical and experimental determination of $\Phi_{\rm Be}$, one requires that the ratio between the two rates for the $^{3}{\rm He} + ^{4}{\rm He}$ and the $^{3}{\rm He} + ^{3}{\rm He}$ reactions,

$$R = \frac{\langle \lambda_{34} \rangle}{\langle \lambda_{33} \rangle},\tag{6}$$

is drastically altered from $R^{\text{SSM}} = 0.16$ to something about R = 0.02 (here and in the following, λ_{ij} is the rate for the collision between nuclei with mass number i and j, m_{ij} being the reduced mass).

The investigation of nonstandard solar models where R is strongly reduced will be the subject of the next sections. It is worth remarking, however, that a reduction of Φ_{Be} to bring it in the experimentally acceptable range generally implies also a comparable, or even larger, re-

TABLE III. Physical input parameters of several standard solar models. We show the solar mass M_0 [10^{33} gr], the solar radius R_0 [10^{10} cm], the solar luminosity L_0 [10^{33} erg/s], the solar age [10^9 yr], the metal to hydrogen mass fraction Z/X, the zero energy astrophysical S factors [MeV barn] and their derivatives with respect to energies S' [barn]. BP is "the best model with diffusion" of Ref. [24]; TCL is the "IS Cpp Recent CNO model" of Ref. [28]; CDF94 is our updated standard solar model, with Livermore opacity table [29], chemical composition following Grevesse 1991 "low iron" [30], and without diffusion.

Physical	BP	TCL	CDF94
quantities			
$\overline{M_0}$	1.989	1.989	1.989
R_0	6.96	6.96	6.96
L_0	3.86	3.85	3.83
Age	4.6	4.5	4.6
Z/X	2.67×10^{-2}	2.43×10^{-2}	2.67×10^{-2}
$\overline{S(0)_{pp}}$	4.00×10^{-25}	4.00×10^{-25}	3.89 ×10 ⁻²
$S'(0)_{pp}$	4.52×10^{-24}	4.67×10^{-24}	4.52×10^{-2}
$S(0)_{33}$	5.00	5.00	5.00
$S'(0)_{33}$	-0.9	-0.9	-0.9
$S(0)_{34}$	5.33×10^{-4}	5.4×10^{-4}	5.33×10^{-4}
$S'(0)_{34}$	-3.1×10^{-4}	-3.10×10^{-4}	-3.10×10^{-4}
$S(0)_{17}$	2.24×10^{-5}	2.24×10^{-5}	2.24×10^{-5}
$S'(0)_{17}$	-3.00×10^{-5}	-3.00×10^{-5}	-3.00×10^{-5}
$S(0)_{^{12}C+p}$	1.45×10^{-3}	1.40×10^{-3}	1.40×10^{-3}
$S'(0)_{^{12}C+p}$	2.45×10^{-3}	4.24×10^{-3}	4.24×10^{-3}
$S(0)_{13}_{\mathrm{C}+p}$	5.50×10^{-3}	5.50×10^{-3}	5.77×10^{-3}
$S'(0)_{13}_{C+p}$	1.34×10^{-2}	1.34×10^{-2}	1.40×10^{-2}
$S(0)_{14}_{N+p}$	3.32×10^{-3}	3.20×10^{-3}	3.32×10^{-3}
$S'(0)_{14}_{N+p}$	-5.91×10^{-3}	-5.71×10^{-3}	-5.91×10^{-3}
$S(0)_{^{15}\mathrm{N}(p,\gamma)^{16}\mathrm{O}}$	6.40×10^{-2}	6.40×10^{-2}	6.40×10^{-2}
$S'(0)_{15}N(p,\gamma)_{16}O$	3.00×10^{-2}	3.00×10^{-2}	3.00×10^{-2}
$S(0)_{15}_{N(p,\alpha)^{12}C}$	7.80×10	5.34×10	7.04×10
$S'(0)_{15}N(p,\alpha)^{12}C$	3.51×10^2		4.21×10^2
$S(0)_{16O+p}$	9.40×10^{-3}	9.40×10^{-3}	9.40×10^{-3}
$S'(0)_{16}_{O+p}$	-2.30×10^{-2}	-2.30×10^{-2}	-2.30×10^{-2}

duction of $\Phi_{\rm B}$, which then becomes too small with respect to the experimental value.

IV. NONSTANDARD SOLAR MODELS WITH LOW CENTRAL TEMPERATURE

Clearly the pp chain can be shifted towards the pp-I termination by lowering the inner temperature T, since the tunneling probability is more reduced for the heavier nuclei:

$$\log\left(\frac{\langle\lambda_{34}\rangle}{\langle\lambda_{33}\rangle}\right) \propto \frac{m_{33}^{1/3} - m_{34}^{1/3}}{(KT)^{1/3}}.$$
 (7)

In order to reduce the inner temperatures one may attempt several manipulations [5]: (i) reduce the metal fraction Z/X; (ii) reduce (by an overall multiplicative factor) the opacity tables; (iii) increase the astrophysical factor S_{pp} of the $p+p \rightarrow d+e+\nu$ reaction; (iv) reduce the Sun age.

Clearly (i) and (ii) work in the direction of getting a more transparent Sun, which implies a lower temperature gradient, a larger energy production region, and consequently smaller inner temperatures. When S_{pp} is increased nuclear fusion gets easier, and the fixed luminosity is obtained with a reduced temperature. A younger Sun is another way to get a Sun cooler in its interior, since the central H abundance is increased and, again, nuclear fusion gets easier.

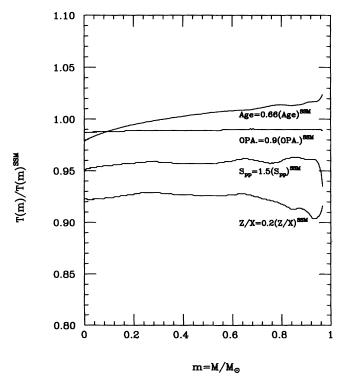


FIG. 5. The temperature profiles T(m) normalized to $T^{\text{SSM}}(m)$ for a few representative nonstandard solar models.

TABLE IV. Comparison among recent standard solar model predictions and experimental results. For the definition of BP, TCL, and CDF94 see Table III. We show the central temperature T_c [10⁷K], the Helium abundance in mass Y, the metallicity fraction Z, the values of each component of the neutrino flux [10⁹ cm⁻² s⁻¹], the calculated signals for the chlorine (Cl) and the gallium (Ga) experiments [SNU]. On the right side we present the experimental constraints at the level of one and three standard deviations.

	St	andard solar mode	els	Experimental constraints			
	BP	TCL	CDF94	1σ	3σ	\mathbf{From}	
T_c	1.569	1.543	1.564		, , , , , , , , , , , , , , , , , , ,		
Y	0.273	0.271	0.289				
$Z~(\times 10^2)$	1.96	1.88	1.84				
pp	60.0	60.4	60.0				
pep	0.14	0.14	0.14				
$pp+\mathrm{pep}$	60.14	60.54	60.14	≥ 64.0	$\geq~61.0$	Ga + Cl	
⁷ Be	4.89	4.25	4.79	≤ 0.70	\leq 4.23	Ga + Cl	
${}^{8}B(\times 10^{3})$	5.69	4.14	5.6	\leq 3.30	\leq 4.10	Ka	
	0.49	0.36	0.47				
¹⁵ O	0.43	0.30	0.40				
$^{13}N + ^{15}O$	0.92	0.66	0.87	≤ 0.6	< 3.6	Ga + Cl	
$^{17}F~(\times 10^3)$	5.4		4.8	_	-		
hep $(\times 10^6)$	1.2		1.3				
Cl	8.0	6.1	7.8	≤ 2.6	≤ 3.0	Cl	
Ga	132	121	130	≤ 88	$\stackrel{-}{\leq} 108$	$_{ m Ga}$	

On the other hand, we remark that variations of the other astrophysical S factors S_{33} , S_{34} , and/or S_{17} affect very weakly the inner solar temperature. This is physically clear, since the energy production mechanism is untouched [6].

We have computed several solar models by varying the parameters well beyond the uncertainties of the standard solar model (see Table V); i.e., we have really built non-standard solar models.

An important feature of all these models is the homology of the inner temperature profiles:

$$T(m) = kT^{\text{SSM}}(m), \tag{8}$$

where $m = M/M_0$ is a mass coordinate, and the factor k depends on the parameter which is varied but does not depend on m.

We have verified that Eq. (8) holds with an accuracy better than 1% in all the internal radiative zone $(M/M_0 < 0.97 \text{ or } R/R_0 < 0.7)$ for all the models we consider, but for huge (and really unbelievable) variations of the solar age, see Fig. 5 and Table V. It is worth remarking that $T(m)/T^{\rm SSM}(m)$ is constant through a re-

TABLE V. Test of the homology relationships. We show $k = \langle T(m)/T(m)^{\rm SSM} \rangle$, and its r.m.s. variation Δk for several nonstandard models, obtained by varying: $s_{pp} = S_{pp}/S_{pp}^{\rm SSM}$, O = Opacity / opacity $S_{pp}^{\rm SSM}$, $z = (Z/X)/(Z/X)^{\rm SSM}$, and $t = {\rm Agg}/S_{pp}^{\rm SSM}$. The averages are performed over the mass shells in the region (a) $M/M_0 \leq 0.3$, and (b) $M/M_0 \leq 0.97$.

					(a)						
S	op variation		Op	acity variat			Z/X variation	on	4	Age variatio	on
s_{pp}	k	Δk	0	k	Δk	z	k	Δk	t	\boldsymbol{k}	Δk
		(10^{-3})			(10^{-3})			(10^{-3})			(10^{-3})
1.25	0.976	1.36	0.9	0.988	0.72	0.5	0.962	1.46	0.9	0.996	2.16
1.5	0.955	2.58	0.7	0.958	2.71	0.3	0.939	2.17	0.7	0.987	6.56
1.75	0.939	3.04	0.6	0.939	3.71	0.2	0.925	2.40	0.4	0.979	10.6
2.0	0.925	3.58				0.1	0.904	4.20	0.2	0.971	14.8
2.5	0.902	4.45							0.1	0.966	17.3
3.5	0.868	5.43									

S	pp variation		Op	acity variat	ion	Z	\mathbb{Z}/X variatio	\mathbf{n}	A	Age variatio	\mathbf{n}
s_{pp}	k	Δk	0	k	Δk	z	k	Δk	t	k	Δk
		(10^{-3})			(10^{-3})			(10^{-3})			(10^{-3})
1.25	0.977	1.82	0.9	0.989	1.07	0.5	0.962	2.80	0.9	1.00	4.17
1.5	0.957	1.88	0.7	0.962	4.00	0.3	0.938	4.48	0.7	1.00	12.8
1.75	0.941	5.00	0.6	0.944	5.17	0.2	0.923	5.98	0.4	0.999	21.0
2.0	0.928	6.48				0.1	0.902	8.45	0.2	1.00	2.97
2.5	0.905	10.3							0.1	1.00	14.8
3.5	0.870	17.4									

gion where T(m) changes by a factor of 5; see Fig. 6.

By looking at the numerical results, one finds, as expected, that, as long as the Sun age is kept fixed, the models have similar distributions of 4 He and of the energy production per unit mass, which as well known, is strongly related to temperature and 4 He density. On the other hand, when the Sun age is varied, the 4 He content also changes strongly, and the homology relation for the temperature is fading away. The important point is that for each model the temperature profile is essentially specified by a scale factor, which can be taken as the central temperature T_c .

On these grounds one derives general predictions for the behavior of the neutrino fluxes Φ_i . They are crucially dependent (through the Gamow factors) on the values of the temperature in the production regions T_i , and, as usual, can be locally approximated by power laws:

$$\Phi_i = c_i \, T_i^{\beta_i}. \tag{9}$$

The homology relationship implies $T_i = (T_c/T_c^{\rm SSM})T_i^{\rm SSM}$ and, consequently,

$$\Phi_{i} = \Phi_{i}^{\text{SSM}} \left(\frac{T_{c}}{T_{c}^{\text{SSM}}} \right)^{\beta_{i}}. \tag{10}$$

This means that each flux is mainly determined by the central temperature, almost independently of the way the temperature variation was obtained, an occurrence which is clearly confirmed by Fig. 7 for the components of the

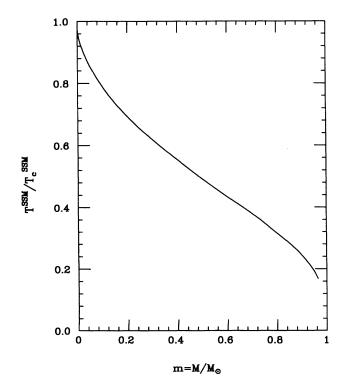


FIG. 6. The SSM temperature profile $T^{\text{SSM}}(m)$, normalized to the central value T_c^{SSM} .

TABLE VI. The β_i coefficients of the power laws that describe the dependence of the neutrino fluxes on the temperature $[\Phi_i = \Phi_i^{\rm SSM}(T_c/T_c^{\rm SSM})^{\beta_i}]$. The components of neutrino flux that we consider are shown in the first column. The values presented are the best fit to the numerical calculations performed when each input parameter is varied in the range specified in the first row (same notation as Table IV).

	s_{pp}	0	z	t
	1-3.5	0.6 - 1	0.1 - 1	0.1 - 1
\overline{pp}	-0.60	-0.63	-0.73	-0.85
$^{7}\mathrm{Be}$	8.74	9.51	10.8	11.4
¹³ N	15.1	12.0	30.9	8.58
¹⁵ O	23.51	15.7	35.6	17.6
рер	2.20	-2.23	-1.71	0.49
8B	22.3	20.76	21.5	20.2

neutrino flux which give the main contributions (Φ_{pp} , Φ_{Be} , and Φ_{B}) to the experimental signals.

The situation is shown in more details in Table VI, where we present the numerically calculated values of the β_i coefficients. One sees that β_{pp} , β_{Be} , and β_{B} are approximately independent of the parameter that is varied. This is not true for Φ_{N} , Φ_{O} , and Φ_{pep} . Actually, when writing Eq. (9) we neglected the flux dependence on the densities of the parent nuclei which generate solar neutrinos. These densities can change when some of the input parameters are varied. For example, Φ_{N} and Φ_{O} look very sensible to variations of Z/X, since in this case,

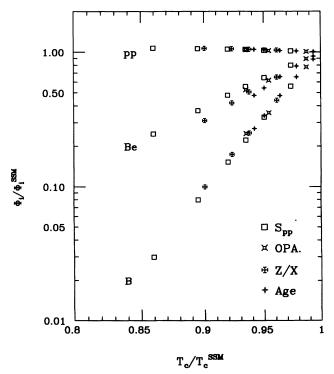


FIG. 7. The behavior of Φ_{pp} , Φ_{Be} , and Φ_{B} as a function of the central temperature T_c when varying S_{pp} , opacity, Z/X, and age.

in addition to the temperature variation, the change of metallicity also influences the effectiveness of the CN cycle. However, this effect is negligible when estimating total experimental signals.

Analytical approximations to the numerical values of the β_i can be found by considering the dependence on temperature of the Gamow factors for the relevant nuclear reactions [20]. We would like to comment here just on the temperature dependence of the ratio $\Phi_{\rm B}/\Phi_{\rm Be}$:

$$\frac{\Phi_{\rm B}}{\Phi_{\rm Be}} = \frac{n_p \langle \sigma_V \rangle_{17}}{n_e \langle \sigma_{V_e} \rangle_{\rm capt}} \propto \frac{n_p}{n_e} \frac{T^{\gamma_{17}}}{T^{\gamma_{\rm capt}}}, \tag{11}$$

where $\gamma_{\rm capt}=-1/2$, and $\gamma_{17}=-2/3+E_{17}/KT$ (E_{17} is the Gamow peak for the $p+{}^7{\rm Be}\to\gamma+{}^8{\rm B}$ reaction) [21]. Assuming n_p/n_e to be constant, and evaluating E_{17}/KT at $T_c^{\rm SSM}$, we get

$$\frac{\Phi_{\rm B}}{\Phi_{\rm Be}} \propto T_c^{13.5}.\tag{12}$$

This value is in good agreement with the one reported in Table VI for a S_{pp} variation; the agreement is less good with the values obtained by varying the other parameters (in this case n_p/n_e is clearly not conserved).

Therefore, as long as the temperature profile is unchanged, lowering the temperature immediately implies that boron neutrinos are suppressed much more strongly than beryllium neutrinos, since the penetrability factor for the $p + {}^{7}\text{Be} \rightarrow \gamma + {}^{8}\text{B}$ reaction is diminished.

V. THE CENTRAL SOLAR TEMPERATURE AND THE EXPERIMENTAL RESULTS

From the argument just presented, it is clear that a central temperature reduction cannot work; nevertheless, let us perform a $\chi^2(T_c)$ analysis to see quantitatively what happens. We define

$$\chi^{2}(T_{c}) = \sum_{XY} (S_{X}^{\text{ex}} - S_{X}^{\text{th}}) V_{XY}^{-1} (S_{Y}^{\text{ex}} - S_{Y}^{\text{th}}), \tag{13}$$

where the symbols have the following meaning.

- (i) The experimental signals $S_X^{\mathbf{x}}$ (X = gallium, chlorine, and Kamiokande) are the ones reported in Eqs. (3) and (4).
- (ii) The theoretical signals $S_X^{
 m th}(T_c)$ are calculated according to the formula

$$S_X^{\text{th}} = \sum_{i \neq pp} X_i \, \Phi_i^{\text{SSM}} \left(\frac{T_c}{T_c^{\text{SSM}}} \right)^{\beta_i} + X_{pp} \, \Phi_i^{pp}, \tag{14}$$

where we take the β coefficients corresponding to the S_{pp} variations (second column of Table VI), and we use our updated standard solar model (column labeled CDF94 in Table IV). Note, in particular, that $\Phi_B^{\rm SSM}$ has been calculated by using $S_{17}=22.4$ eV barn. In order to achieve a better accuracy, Φ_{pp} is calculated directly through the Eq. (1).

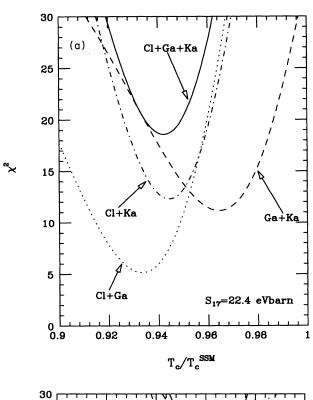
(iii) The error matrix V_{XY} takes into account both

the experimental and the theoretical uncertainties. The theoretical uncertainties are due to the neutrino cross sections X_i , and to the solar model parameters that are not related to the free parameter T_c , i.e., S_{33} , S_{34} , and S_{17} . The diagonal entries, V_{XX} , are the sum of the experimental variance σ_X^2 , plus the squares of the errors due to the cross sections $\sum_{i} (\Delta_X^i)^2 (\Delta_X^i)$ is the error of the detection cross section for the X experiment averaged over the ith flux), plus the squares of the errors due to the input parameters S_{33} , S_{34} , and S_{17} , i.e., $\sum_{P} (\Delta_X^P)^2$ ($P = \hat{S}_{33}, S_{34}, S_{17}$). The off-diagonal entries have contributions only from these last errors: $V_{XY} = \sum_{P} \Delta_{X}^{P} \Delta_{Y}^{P}$. The errors Δ are calculated by linear propagation. Therefore, if we call δ_{X}^{i} the error on the cross section X_{i} , $\Delta_{X}^{i} = \Phi_{i}^{\text{SSM}} \left(\frac{T_{c}}{T_{c}^{\text{SSM}}}\right)^{\beta_{i}} \delta_{X}^{i}$, while, if δ^{P} is the error on the parameter P, $\Delta_{X}^{P} = \left(\partial S_{X}^{\text{th}}/\partial P\right) \delta^{P}$. The partial derivatives of the neutrino fluxes with respect to these parameters are estimated by using power laws which we have been determined from numerical experiments, and which are very similar to those of Table 7.2 in Ref. [22]. The values we use for the uncertainties of the SSM parameters, δ^{P} , are given in Table I, while the errors on the cross sections, δ_X^i , can be found in Table II. The use of the error matrix is necessary to avoid that an apparently good fit be achieved in an unphysical way; e.g., we cannot use the uncertainty of the boron flux to strongly reduce its contribution to the Davis experiment, and, at the same time, have a smaller reduction in the Kamiokande experiment.

The results shown in Fig. 8(a) deserve a few comments.

- (i) The best fit to the three experimental signals yields a $\chi^2_{\min}[\text{Cl+Ga+Ka}]=18.5$ that, for two degrees of freedom, is excluded at the 99.99% level (here we have treated systematic and statistical errors on equal footing); we thus confirm the results of Refs. [23,8]. This is partly due to the well known "inconsistency" between Kamiokande and chlorine.
- (ii) Even if we only consider gallium and Kamiokande the fit is still poor, yielding a $\chi^2_{\min}[Ga+Ka]=11$, that for one degree of freedom is excluded at the 99.9% level. The reason is that if one tries to reduce Φ_{Be} in accordance with gallium data, then Φ_{B} becomes too small in comparison with the Kamiokande result. On the other hand, if one considers just gallium and chlorine results the situation is better $(\chi^2_{\min}[Cl+Ga]=5$, which has a 2.5% probability), due to the fact that the smaller boron (and beryllium) signal implied by the chlorine experiment can be more easily adjusted to the gallium result.
- (iii) From the above discussion it is clear that if one lowers the $p + {}^{7}\text{Be} \rightarrow \gamma + {}^{8}\text{B}$ cross section, the situation gets even worse, see Fig. 8(b). In other words, a reduction of S17 does not solve the solar neutrino problem.
- (iv) Considering the chlorine data corresponding (approximately) to the same data taking period as the other experiments ($S_{\rm Cl}^{88-92}=2.76\pm0.31~{\rm SNU}$ [3]) the situation is only slightly changed: $\chi^2_{\rm min}[{\rm Cl+Ga+Ka}]=15~{\rm that}$, for two degrees of freedom, is excluded at the 99.94% level; $\chi^2_{\rm min}[{\rm Ga+Ka}]=11$, that for one degree of freedom is excluded at the 99.9% level; and $\chi^2_{\rm min}[{\rm Cl+Ga}]=6$, which has a 2.4% probability.

(v) For the uncertainties of Table I, the effect of the error correlation is not large: for instance, if we use uncorrelated errors $\chi^2_{\min}[\text{Cl+Ga+Ka}]=16$ instead of 18.5. The real importance of error correlation becomes evident



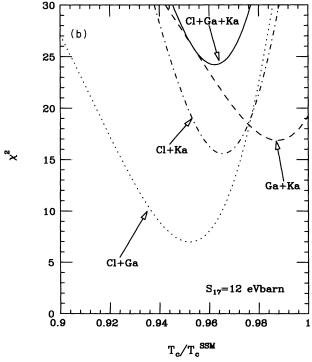


FIG. 8. The χ^2 as a function of the central temperature T_c . (a) We use the standard value $S_{17}=22.4$ eV barn [31]. (b) We use the recently proposed value $S_{17}=12$ eV barn [9].

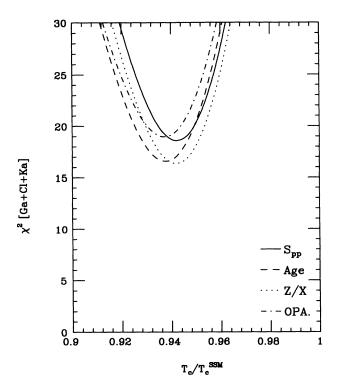


FIG. 9. The χ^2 as a function of the central temperature T_c when the temperature variation is obtained by changing the different input parameters.

if we try to resolve the discrepancy by increasing the errors. For example, doubling the uncertainties reduces the uncorrelated χ^2_{\min} to 14, while the correlated one practically does not change.

(vi) The situation does not significantly change when considering models where one of the other parameters (opacity table, Z/X, age) are varied instead of S_{pp} , as it is shown by Fig. 9. Slightly better fits are obtained by varying Z/X or the age than S_{pp} or the opacities, but the resulting $\chi^2_{\min}[\text{Cl+Ga+Ka}]=16.5$ is still excluded at the 99.97% level.

(vii) If one insists on a low temperature solution, the best fit is for $T_c/T_c^{\rm SSM}\approx 0.94$, i.e., $T_c=1.46\times 10^7$ K. The price to pay for this 6% temperature reduction is very high in terms of the input parameters which are being varied; see Table I. Huge variations of the parameters are required, and, furthermore, in many cases the values used are at the border of what can be tolerated by our stellar evolution code: for example, we are not able to produce a Sun with $T_c/T_c^{\rm SSM}<0.94$ by lowering the opacity or the age.

VI. A LOW ENERGY RESONANCE IN THE ³He + ³He CHANNEL?

As mentioned in the Introduction, the other way to enhance the pp-I termination is to play with the ³He nuclear cross sections. As was shown in Ref. [6], if the astrophys-

ical S factors are varied by a constant (through the star) quantity,

$$\Phi_i = \Phi_i^{\text{SSM}} \theta, \tag{15a}$$

where

$$\theta = \frac{S_{34}}{S_{34}^{\text{SSM}}} \sqrt{\frac{S_{33}^{\text{SSM}}}{S_{33}}}$$
 and $i = \text{B, Be.}$ (15b)

Numerical experiments confirm the approximate validity of Eqs. (15) giving $\Phi_{B,Be} = \Phi_{B,Be}^{SSM} \theta^{0.9}$. Note that the changes of Φ_{B} and Φ_{Be} are proportional.

For variations of S_{33} and S_{34} the solar temperature is essentially unaffected, and, consequently, all the fluxes other than B and Be are also unaffected. Only the pp+pep neutrino flux changes slightly, in order to satisfy the luminosity condition, Eq. (1): i.e.,

$$\Phi_{pp+pep} = \Phi_{pp+pep}^{SSM} + \Phi_{Be}^{SSM} - \Phi_{Be}. \tag{16}$$

In order to reduce the beryllium flux by a factor, say, three, with respect to the SSM value, S_{33} (S_{34}) has to be nine times (one-third) the value used in the standard solar model calculations. Clearly, what matter are the values of the astrophysical factors at the energies relevant in the Sun, i.e., at the position of the Gamow peak for the He + He reactions near the solar center, $E_G \approx 20$ keV.

We recall that the astrophysical factors used in the calculations are obtained by extrapolating experimental data taken at higher energies (see Ref. [21] for a review). Thus a very low energy resonance in the ${}^{3}\text{He} + {}^{3}\text{He}$ reactions could be effective in reducing Φ_{Be} and Φ_{B} , and could have escaped experimental detection. This possibility, first advanced in Ref. [11], cannot be completely dismissed (see the discussion in Refs. [6,21]) and it is presently being investigated in the underground nuclear physics experiment LUNA at Laboratori Nazionali del Gran Sasso [12].

For a resonance at energy E_r and with strength $\omega \gamma$, Eqs. (15) become

$$\Phi_i = \Phi_i^{\text{SSM}} \sqrt{\frac{1}{1 + x_i}} \qquad i = B, Be, \qquad (17a)$$

where

$$x_i = \frac{\omega \gamma}{W} \exp[3A(KT_i)^{-1/3} - E_r/(KT_i)],$$
 (17b)

and T_i are the temperatures at the peak of the $\nu_{\rm Be}$ and $\nu_{\rm B}$ production ($T_{\rm Be}=1.45\times10^7$ K, $T_{\rm B}=1.5\times10^7$ K), K is the Boltzmann constant, and the other constants, defined in Ref. [6], are W=20.4 keV and A=1.804 MeV^{1/3}.

Let us remark that the resonance can work differently in different regions of the Sun, in relationship with the kinetic energies of the colliding particles. A low energy resonance is more efficient in the outer zone of energy production, and consequently $\Phi_{\rm Be}$ can be suppressed more than $\Phi_{\rm B}$. The opposite occurs for higher energy resonances, the turning point being $E_r \approx E_G$; see Ref. [6] for details.

We have performed a χ^2 analysis as a function of the

resonance strength $\omega \gamma$ for several values of the resonance energy E_r , with a procedure quite similar to that used in the preceding section.

The errors on the calculated signals arise from the neutrino interaction cross sections, from S_{17} , and from all those quantities which influence the estimated central temperature of the Sun $(S_{pp}, Z/X)$, opacity, and age), but not from S_{33} and S_{34} that influence fluxes according to Eq. (15), and correspond to our free parameter. Again, the derivative of the neutrino fluxes with respect to these parameters, necessary to calculate the error matrix by linear propagation, are estimated by using power laws very similar to those of Table 7.2 in Ref. [22].

The uncertainties we use are shown in Tables I and II. We note that uncertainties on the absorption cross sections, the metallicity Z/X, and the opacity are the most important for estimating the errors on the signal. For the opacity we followed Ref. [24] and took "the characteristic difference between the solar interior opacity calculated with Livermore and with Los Alamos opacity code," which may or may not be a fair estimate of the uncertainty, but we could not find a better prescription. However, as we shall see, the correlation among the errors is such that χ^2_{\min} does not change even if we double the uncertainties on Z/X and on the opacity.

The results are presented in Fig. 10. The situation looks slightly better than in the low temperature models since the $\Phi_{\rm Be}$ reduction does not imply an even stronger $\Phi_{\rm B}$ reduction. However, the best $\chi^2_{\rm min}=14$, obtained for $E_r=0$, is still excluded at the 99.9% level. The $\chi^2_{\rm min}$

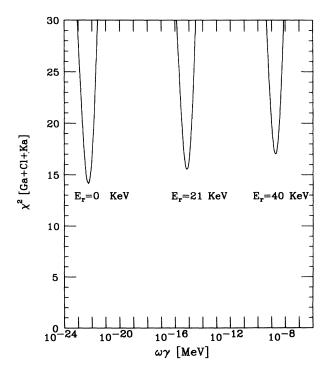


FIG. 10. For a few values of the resonance energy E_r , we show χ^2 as a function of the resonance strength $\omega \gamma$. The fit is done with all (Ga+Cl+Ka) data.

slightly increases with E_r because of the tuning of the ratio of the beryllium and boron suppressions.

The best fit strength as a function of E_r is shown in Fig. 11, together with existing experimental upper bound. We expect that LUNA experiment, presently performed at LNGS [12], will have a sensitivity better by about a factor 100, as compared with previous experiments, mainly due to the cosmic ray shielding in the underground laboratory, so that the search should be able to detect/exclude such a resonance down to extremely low values of E_r .

The use of the properly correlated errors on the fluxes is even more important when studying the effect of the hypothetical resonance than when we changed the temperature. The χ^2_{\min} would be 10 instead of 14, had we used uncorrelated errors. Moreover, doubling the errors would yield a χ^2_{\min} of almost 6, while the correlated one remains 14. The intuitive explanation of how the uncorrelated fit works is the following. The chlorine and Kamiokande results require different suppressions of the neutrino fluxes. The fit finds the best compromise between the two experiments by adjusting the resonance strength. Then, the uncertainty on the temperature is used to further deplete Φ_{Be} and, at the same time, to increase $\Phi_{\rm B}$, which is clearly unphysical. The correlated fit correctly uses the uncertainty on the temperature either to increase or to decrease both fluxes at the same time: either option is useless, once we get the best compromise

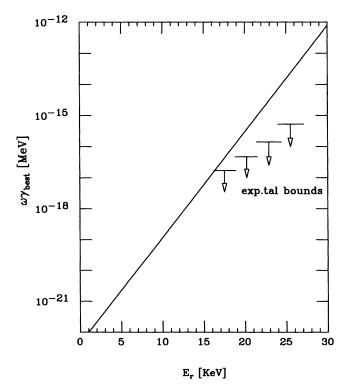


FIG. 11. The best fit strength $\omega \gamma$ of the ³He + ³He resonances as a function of the resonance energy E_r (full line). The arrows correspond to the experimental upper bounds on the resonance strength, from Ref. [32].

for the common reduction of the two fluxes, no matter how much we are allowed to change the temperature.

Combining the two mechanisms, i.e., a resonance in a low temperature model, does not work either, since again, once the best compromise suppression of the ⁷Be and ⁸B fluxes is achieved by one of the two mechanisms, the other cannot do much more.

VII. THE DETECTION OF pep AND ⁷Be NEUTRINOS

New generation experiments are being planned for the detection of monochromatic solar neutrinos produced in electron capture (${}^{7}\text{Be} + e^{-} \rightarrow {}^{7}\text{Li} + \nu$) and in the pep $(p+e^{-}+p \rightarrow d+\nu)$ reactions [13–15]. Furthermore, Bahcall [16,17] pointed out that, from the measurement of the average energy difference between neutrinos emitted in solar and laboratory decay, one can infer the temperature of the production zone. In this section we discuss what can be learned from such future measurements about the properties of neutrinos and of the Sun.

Concerning the intensity of the ⁷Be line, we recall the

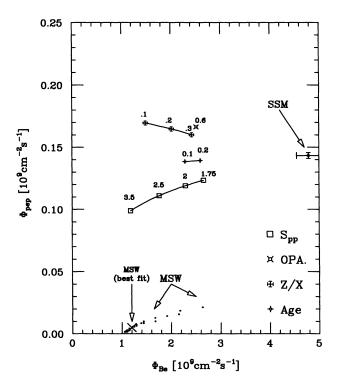


FIG. 12. The pep neutrino flux (Φ_{pep}) vs the ⁷Be neutrino flux (Φ_{Be}) . For the standard solar model (\diamondsuit) . For several nonstandard solar models adjusted so as to reproduce the gallium result within 3σ (the boron contribution is taken from the Kamiokande experiment); the notation is as in Fig. 7, and the number close to each point represents the corresponding value of $\zeta = P/P^{\text{SSM}}$. The values for the MSW solution, corresponding to the best fit (\times) , and to the 90% confidence level region (dots); see also Ref. [33].

bounds of Eqs. (5): at 1σ (3 σ) the neutrino flux has to be smaller than 0.7×10^9 cm⁻² s⁻¹ (4.0 × 10^9 cm⁻² s⁻¹), otherwise neutrinos are nonstandard. We recall however that a low $\Phi_{\rm Be}$ is also typical of the Mikheyev-Smirnov-Wolfenstein (MSW) solution; see Fig. 12.

The pep neutrinos are a good indicator of Φ_{pp} , since the ratio Φ_{pep}/Φ_{pp} is rather stable. In Fig. 12 we see that standard neutrinos correspond to Φ_{pep} in the range $(1-2)\times 10^8$ cm⁻² s⁻¹, whereas the MSW solution requires $\Phi_{pep} \leq 3\times 10^7$ cm⁻² s⁻¹. Thus, a measurement of the pep line intensity will be crucial for deciding about neutrino properties.

The possibility of measuring inner solar temperatures through thermal effects on monochromatic neutrino lines looks to us extremely fascinating (although remote). In this respect the homology relationship, Eq. (8), is particularly interesting; see Fig. 13.

If homology holds, a measurement of the solar temperature in the, say, $^7\mathrm{Be}$ production zone gives the value of T_c . On the other hand, the homology relation itself is testable, in principle, by comparing the temperatures at two different places, as can be done by looking at the shapes of both the ν_{Be} and ν_{pep} lines. We remark that this would be a test of the mechanism for energy transport through the inner Sun.

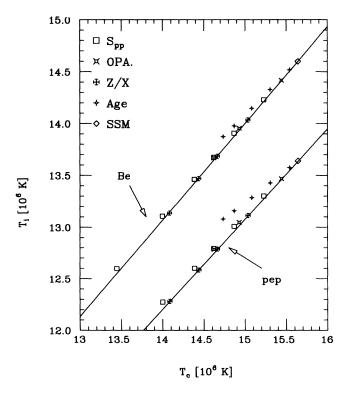


FIG. 13. Relations among the temperatures T_i at the ⁷Be and pep peak production zones $(R/R_0=0.06$ and $R/R_0=0.09$, respectively), and the central temperature T_c in nonstandard solar models. Data from numerical calculations are shown with the same symbols as in Fig. 7, while full lines show the homology relations $T_i=T_c\,(T_i^{\rm SSM}/T_c^{\rm SSM})$.

VIII. CONCLUSIONS

(i) If neutrinos are standard, the present solar neutrino experiments already impose severe constraints on the individual components of the total neutrino flux. These constraints, at the 1σ level, are

$$\begin{split} \Phi_{\text{Be}} & \leq 0.7 \times 10^9 \text{ cm}^{-2} \text{ s}^{-1}, \\ \Phi_{\text{CNO}} & \leq 0.6 \times 10^9 \text{ cm}^{-2} \text{ s}^{-1}, \\ 64 \times 10^9 \text{ cm}^{-2} \text{ s}^{-1} & \leq \Phi_{pp+pep} \leq 65 \times 10^9 \text{ cm}^{-2} \text{ s}^{-1}. \end{split} \tag{18}$$

The constraint on beryllium neutrinos is in strong disagreement with the results of any standard solar model calculation; see Table IV. The solar neutrino problem is now at the beryllium production level: the experimental data demand a strong shift towards the *pp*-I termination, and the problem is not restricted anymore to the rare *pp*-III (⁸B) termination.

- (ii) Solar models with low inner temperatures show temperature profiles T(m) homologous to that of the standard solar model: $T(m) = kT^{\rm SSM}(m)$. As a consequence, the main components of the neutrino flux depend essentially on the central solar temperature T_c (see Table V), and the experimental signals can be parameterized in terms of T_c . As already known, there is no value of T_c which can account for all the available experimental results $\left[\chi^2_{\min}(T_c)\approx 16\right]$. In addition, we find that the fit is poor even considering just gallium and Kamiokande results $\left[\chi^2_{\min}(T_c)\approx 11\right]$. Furthermore, lowering the cross section for $p+{}^7{\rm Be} \to \gamma + {}^8{\rm B}$ makes things worse.
- (iii) Alternatively, the shift of the nuclear fusion chain towards the pp-I termination could be induced by a hypothetical low energy resonance in the $^3{\rm He} + ^3{\rm He}$ reaction. This mechanism gives a somehow better but still poor fit to the combined experimental data $[\chi^2_{\rm min}(T_c) \approx 14]$. Its possible relevance to the solar neutrino problem will be elucidated in an underground nuclear physics experiment, presently performed at LNGS.
- (iv) Concerning future experiments, the measurement of the ⁷Be and, particularly, of the pep line intensities will be crucial for discriminating nonstandard solar models from nonstandard neutrinos, in relation with the bounds in Eq (18). Furthermore, the homology relation itself can be tested, in principle, in experiments aimed at the measurement of inner solar temperatures by looking at thermal effects on the pep and Be line shapes. This would provide a clear test about the mechanism of energy transport in the solar interior.

In conclusion, we feel that recent gallium results, taken at their face value, strongly point towards nonstandard neutrinos. Of course we are anxiously waiting for the calibration of GALLEX and SAGE, and for future experiments.

ACKNOWLEDGMENT

One of us (G.F.) acknowledges useful discussions with V. Berezinsky.

- GALLEX Collaboration, P. Anselman *et al.*, Phys. Lett. B **327**, 377 (1994).
- [2] V. N. Gavrin, in presentation given at 6th International Symposium on Neutrino Telescopes, Venice, Italy, February, 1994 (unpublished).
- [3] R. Davis, Jr., in Proceedings of the 23rd International Cosmic Ray Conference, Calgary, Canada, 1993, edited by D. A. Leahy (University of Calgary, Calgary, 1993); Prog. Nucl. Part. Phys. 32, 1 (1994).
- [4] A. Suzuki, in [2].
- [5] V. Castellani et al., Phys. Lett. B 324, 245 (1994).
- [6] V. Castellani, S. Degl'Innocenti, and G. Fiorentini, Astron. Astrophys. 271, 601 (1993).
- [7] S. A. Bludman et al., Phys. Rev. D 45, 1810 (1992).
- [8] N. Hata, "Solar neutrinos: hint for neutrino mess," University of Pennsylvania Report No. UPR-0612T (unpublished).
- [9] K. Langanke and T. D. Shoppa, Phys. Rev. C 49, 1771 (1994).
- [10] T. Motobayashi et al., Rikkyo Report No. RUP-94/2, 1994 (unpublished).
- [11] W. A. Fowler, Nature 238, 24 (1972).
- [12] C. Arpesella et al., "Nuclear Astrophysics at Gran Sasso Laboratory" (proposal for a pilot project with a 30 KeV accelerator), Report No. LNGS 91-18, 1991 (unpublished).
- [13] C. Arpesella et al., "Borexino at Gran Sasso: Proposal for a Real-Time Detector for Low Energy Solar Neutrinos," Report No. INFN - Milan (1992).
- [14] A. Alessandrello et al., "A cryogenic experiment for solar neutrino spectroscopy and search for dark matter," Report No. INFN/AE-92/28, 1992 (unpublished).
- [15] R. S. Raghavan et al., "High resolution spectroscopy of solar neutrinos by neutral and charged currents via ⁷Li

- bolometry," AT&T Bell Laboratories Technical Memorandum 11121-930824-27TM, 1993 (unpublished).
- [16] J. N. Bahcall, Phys. Rev. Lett. 71, 2369 (1993).
- [17] J. N. Bahcall, Phys. Rev. D 49, 3923 (1994).
- [18] N. Hata, S. A. Bludman, and P. Langacker, Phys. Rev. D 49, 3622 (1994).
- [19] V. Berezinsky, "On the exclusion of an astrophysical solution to the solar neutrino problem," INFN – Laboratori Nazionali del Gran Sasso Report Nos. LNGS-93/86 and BONN-HE-93-50 (unpublished).
- [20] V. Castellani, S. Degl'Innocenti, and G. Fiorentini, Phys. Lett. B 303, 68 (1993).
- [21] C. Rolfs and W. Rodney, Cauldrons in the Cosmos (Chicago University Press, Chicago, 1988).
- [22] J. N. Bahcall, Neutrino Astrophysics (Cambridge University Press, Cambridge, England, 1989).
- [23] S. A. Bludman et al., Phys. Rev. D 47, 2220 (1993).
- [24] J. N. Bahcall and M. H. Pinsonneault, Rev. Mod. Phys. 60, 297 (1992).
- [25] J. N. Bahcall and M. Kamionkowski, Astrophys. J. 420, 884 (1994).
- [26] S. Turck-Chièze et al., Phys. Rep. 230, 57 (1993).
- [27] A. Garcia et al., Phys. Rev. Lett. 67, 3654 (1991).
- [28] S. Turck-Chièze and I. Lopez, Astrophys. J. 408, 347 (1993).
- [29] R. Iglesias and Wilson, Astrophys. J. 397, 717 (1992).
- [30] N. Grevesse, in Proceedings of Evolution of Stars: the Photospheric Abundance Connection, International Astronomical Union, 1991, edited by G. Michaud and A. Tutukov (unpublished).
- [31] C. W. Johnson et al., Astrophys. J. 392, 320 (1992).
- [32] A. Krauss et al., Nucl. Phys. A 467, 273 (1987).
- [33] G. Fiorentini et al., Phys. Rev. D 49, 6298 (1994).