Measurement of the Total Active ⁸B Solar Neutrino Flux at the Sudbury Neutrino Observatory with Enhanced Neutral Current Sensitivity

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The Sudbury Neutrino Observatory has precisely determined the total active $(\nu_x)^8 B$ solar neutrino flux without assumptions about the energy dependence of the ν_e survival probability. The measurements were made with dissolved NaCl in heavy water to enhance the sensitivity and signature for neutral-current interactions. The flux is found to be $5.21 \pm 0.27 (\mathrm{stat}) \pm 0.38 (\mathrm{syst}) \times 10^6 \ \mathrm{cm}^{-2} \ \mathrm{s}^{-1}$, in agreement with previous measurements and standard solar models. A global analysis of these and other solar and reactor neutrino results yields $\Delta m^2 = 7.1^{+1.2}_{-0.6} \times 10^{-5} \ \mathrm{eV}^2$ and $\theta = 32.5^{+2.4}_{-2.3}$ degrees. Maximal mixing is rejected at the equivalent of 5.4 standard deviations.

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The Sudbury Neutrino Observatory (SNO) [1] detects ⁸B solar neutrinos through the reactions

$$\nu_e + d \rightarrow p + p + e^-$$
 (CC), $\nu_x + d \rightarrow p + n + \nu_x$ (NC), $\nu_x + e^- \rightarrow \nu_x + e^-$ (ES).

Only electron neutrinos produce charged-current interactions (CC), while the neutral-current (NC) and elastic

scattering (ES) reactions have sensitivity to nonelectron flavors. The NC reaction measures the total flux of all active neutrino flavors above a threshold of 2.2 MeV.

SNO previously measured the NC rate by observing neutron captures on deuterons, and found that a standard-model description with an undistorted 8B neutrino spectrum and CC, ES, and NC rates due solely to ν_e interactions was rejected [2,3]. This Letter presents measurements of the CC, NC, and ES rates from SNO's dissolved salt phase.

The addition of NaCl, 0.195% by weight, to the 1-Gg heavy-water target increased the neutron capture efficiency and the associated Cherenkov light. The solution was thoroughly mixed and a conductivity scan along the vertical axis showed the NaCl concentration to be uniform within 0.5%.

The data presented here were recorded between July 26, 2001 and October 10, 2002, totaling 254.2 live days. The number of raw triggers was 435×10^6 and the data set was reduced to 3055 events after data reduction similar to that in [3] and analysis selection requirements. Cherenkov event backgrounds from β - γ decays were reduced with an effective electron kinetic energy threshold $T_{\rm eff} \geq 5.5$ MeV and a fiducial volume with radius $R_{\rm fit} \leq 550$ cm.

The neutron detection efficiency and response were calibrated with a ²⁵²Cf neutron source. The neutron capture efficiency is shown in Fig. 1(a). The detection efficiency for NC reactions in the heavy water was 0.399 ± 0.010 (calibration) ± 0.009 (fiducial volume) for $T_{\rm eff} \geq 5.5~{\rm MeV}$ and $R_{\rm fit} \leq 550~{\rm cm}$, an increase of approximately a factor of 3 from the pure D_2O phase. Calibration of the detector's optical and energy response has been updated to include time variation of the water transparency measurements made at various wavelengths throughout the running period. A normalization for photon detection efficiency based on ¹⁶N calibration data [4] and Monte Carlo calculations was used to set the absolute energy scale. ¹⁶N data taken throughout the running period verified the gain drift (approximately 2% per year) predicted by Monte Carlo calculations based on the optical measurements. The energy response for electrons is characterized by a Gaussian function with resolution $\sigma_T = -0.145 + 0.392\sqrt{T_e} + 0.0353T_e$, where T_e is the electron kinetic energy in MeV. The energy scale uncertainty is 1.1%.

Neutron capture on 35 Cl typically produces multiple γ rays while the CC and ES reactions produce single electrons. The greater isotropy of the Cherenkov light from neutron capture events relative to CC and ES events allows good statistical separation of the event types. This separation allows a precise measurement of the NC flux to be made independent of assumptions about the CC and ES energy spectra.

The degree of the Cherenkov light isotropy is reflected in the pattern of photomultiplier tube (PMT) hits. Event

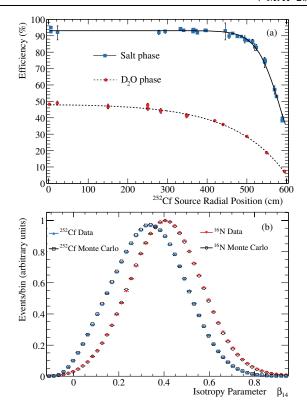


FIG. 1 (color). (a) Neutron capture efficiency versus source radial position for the pure D_2O phase (capture on D) and salt phase (capture on Cl or D) deduced from a ^{252}Cf source, with fits to an analytic function (salt) and to a neutron diffusion model (D_2O). (b) Event isotropy from data and Monte Carlo calculations of a ^{252}Cf source and an ^{16}N γ -ray source.

isotropy was characterized by parameters β_l , the average value of the Legendre polynomial P_l of the cosine of the angle between PMT hits [5]. The combination $\beta_1 + 4\beta_4 \equiv \beta_{14}$ was selected as the measure of event isotropy to optimize the separation of NC and CC events. Systematic uncertainty on β_{14} distributions generated by Monte Carlo for signal events was evaluated by comparing ¹⁶N calibration data to Monte Carlo calculations [6] for events throughout the fiducial volume and running period. The uncertainty on the mean value of β_{14} is 0.87%. Comparisons of β_{14} distributions from ^{16}N events and neutron events from ²⁵²Cf to Monte Carlo calculations are shown in Fig. 1(b). The Monte Carlo calculations of β_{14} have also been verified with 19.8 MeV γ -ray events from a ${}^{3}\text{H}(p, \gamma)^{4}\text{He source [7]}$, high-energy electron events (dominated by CC and ES interactions) from the pure D_2O phase of the experiment, neutron events following muons, and with low-energy calibration sources.

Backgrounds are summarized in Table I. Low levels of the U and Th progeny 214 Bi and 208 Tl can create free neutrons from deuteron photodisintegration and lowenergy Cherenkov events from β - γ decays. Ex situ assays and in situ analysis techniques were employed to

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TABLE I. Background events. The internal neutron and γ -ray backgrounds are constrained in the analysis. The external-source neutrons are reported from the fit. The last two entries are included in the systematic uncertainty estimates.

Source	Events
Deuteron photodisintegration	$73.1^{+24.0}_{-23.5}$
$^{2}\mathrm{H}(\alpha,\alpha)pn$	2.8 ± 0.7
$^{17,18}\mathrm{O}(lpha,n)$	1.4 ± 0.9
Fission, atmospheric ν (NC plus sub-Cherenkov threshold CC)	23.0 ± 7.2
Terrestrial and reactor $\bar{\nu}$'s	2.3 ± 0.8
Neutrons from rock	≤ 1
²⁴ Na activation	8.4 ± 2.3
n from CNO ν 's	0.3 ± 0.3
Total internal neutron background	$111.3^{+25.3}_{-24.9}$
Internal γ (fission, atmospheric ν)	5.2 ± 1.3
¹⁶ N decays	<2.5 (68% C.L.)
External-source neutrons (from fit)	$84.5^{+34.5}_{-33.6}$
Cherenkov events from β - γ decays	<14.7 (68% C.L.)
AV events	<5.4 (68% C.L.)

determine the average levels of uranium and thorium during the experiment [3,8–10]. Results from these methods are consistent. For the 232 Th chain, the weighted mean of the *ex situ* MnO_x and the *in situ* measurement was used. The 238 U chain activity is dominated by Rn ingress, which is highly time variable. The *in situ* determination was used to estimate this background, because it provides the appropriate time weighting. The average rate of background neutron production from activity in the D₂O region is $0.72^{+0.24}_{-0.23}$ neutrons per day.

Backgrounds from atmospheric neutrino interactions and ²³⁸U fission were estimated with the aid of the code NUANCE [11] and from event multiplicities.

 24 Na (which originates from neutron activation of 23 Na) can also emit γ rays which photodisintegrate the deuteron. Residual activation after calibrations and 24 Na production in the water circulation system and in the heavy water in the "neck" of the vessel were determined and are included in Table I. SNO is slightly sensitive to solar CNO neutrinos from the electron-capture decay of 15 O and 17 F.

Neutrons and γ rays produced at the acrylic vessel and in the light water can propagate into the fiducial volume. Radon progeny deposited on the surfaces of the vessel during construction can initiate (α, n) reactions on 13 C, 17 O, and 18 O, and external γ rays can

TABLE II. Systematic uncertainties on fluxes for the spectral shape unconstrained analysis of the salt data set. * denotes CC versus NC anticorrelation.

Source	NC uncertainty (%)	CC uncertainty (%)	ES uncertainty (%)
Energy scale	-3.7, +3.6	-1.0, +1.1	±1.8
Energy resolution	±1.2	± 0.1	± 0.3
Energy nonlinearity	± 0.0	-0.0, +0.1	± 0.0
Radial accuracy	-3.0, +3.5	-2.6, +2.5	-2.6, +2.9
Vertex resolution	± 0.2	± 0.0	± 0.2
Angular resolution	± 0.2	± 0.2	± 2.4
Isotropy mean*	-3.4, +3.1	-3.4, +2.6	-0.9, +1.1
Isotropy resolution	± 0.6	± 0.4	± 0.2
Radial energy bias	-2.4, +1.9	± 0.7	-1.3, +1.2
Vertex Z accuracy*	-0.2, +0.3	± 0.1	± 0.1
Internal background neutrons	-1.9, +1.8	± 0.0	± 0.0
Internal background γ 's	± 0.1	± 0.1	± 0.0
Neutron capture	-2.5, +2.7	± 0.0	± 0.0
Cherenkov backgrounds	-1.1, +0.0	-1.1, +0.0	± 0.0
AV events	-0.4, +0.0	-0.4, +0.0	± 0.0
Total experimental uncertainty	-7.3, +7.2	-4.6, +3.8	-4.3, +4.5
Cross section [13]	±1.1	±1.2	±0.5

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photodisintegrate deuterium. The enhanced neutron capture efficiency of salt makes these external-source neutrons readily apparent, and an additional distribution function was included in the analysis to extract this component (Table I). Previous measurements [2,3,12] with pure D_2O were less sensitive to this background source, and a preliminary evaluation indicates the number of these background events was within the systematic uncertainties reported.

The backgrounds from Cherenkov events inside and outside the fiducial volume were estimated using calibration source data, measured activity, Monte Carlo calculations, and controlled injections of Rn into the detector. These backgrounds were nearly negligible above the analysis energy threshold and within the fiducial volume, and are included as an uncertainty on the flux measurements.

A class of background events identified and removed from the analysis in the pure D_2O phase ("AV events") reconstruct near the acrylic vessel and were characterized by a nearly isotropic light distribution. Analyses of the pure D_2O and salt data sets limit this background to 5.4 events (68% C.L.) for the present data.

To minimize the possibility of introducing biases, a blind analysis procedure was used. The data set used during the development of the analysis procedures and the definition of parameters excluded an unknown fraction (<30%) of the final data set, included an unknown admixture of muon-following neutron events, and included an unknown NC cross section scaling factor. After fixing all analysis procedures and parameters, the blindness constraints were removed. The analysis was then performed on the "open" data set, statistically separating events into CC, NC, ES, and external-source neutrons using an extended maximum likelihood analysis based on the distributions of isotropy, cosine of the event direction relative to the vector from the Sun $(\cos\theta_{\odot})$, and radius within the detector. This analysis differs from the analysis of the pure D₂O data [2,3,12] since the spectral distributions of the ES and CC events are not constrained to the ⁸B shape, but are extracted from the data. The extended maximum likelihood analysis yielded $1339.6^{+63.8}_{-61.5}$ CC, $170.3^{+23.9}_{-20.1}$ ES, $1344.2^{+69.8}_{-69.0}$ NC, and $84.5^{+34.5}_{-33.6}$ external-source neutron events. The systematic uncertainties on derived fluxes are shown in Table II. The isotropy, $\cos\theta_{\odot}$, and kinetic energy distributions for the selected events are shown in Fig. 2, with statistical uncertainties only. A complete spectral analysis including the treatment of differential systematic uncertainties will be presented in a future report. The volume-weighted radial distributions $[\rho = (R_{\rm fit}/600 \text{ cm})^3]$ are shown in Fig. 3.

The fitted numbers of events give the equivalent 8B fluxes [14,15](in units of 10^6 cm⁻² s):

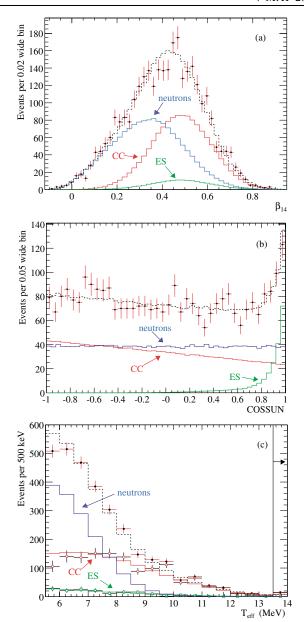


FIG. 2 (color). Distribution of (a) β_{14} , (b) $\cos\theta_{\odot}$, and (c) kinetic energy, for the selected events. The CC and ES spectra are extracted from the data using β_{14} and $\cos\theta_{\odot}$ distributions in each energy bin. Also shown are the Monte Carlo predictions for CC, ES, NC plus internal- and external-source neutron events, all scaled to the fit results. The dashed lines represent the summed components. All distributions are for events with $T_{\rm eff} \geq 5.5$ MeV and $R_{\rm fit} \leq 550$ cm. Differential systematics are not shown.

$$\phi_{\text{CC}}^{\text{SNO}} = 1.59_{-0.07}^{+0.08} (\text{stat})_{-0.08}^{+0.06} (\text{syst}),$$

$$\phi_{\text{ES}}^{\text{SNO}} = 2.21_{-0.26}^{+0.31} (\text{stat}) \pm 0.10 (\text{syst}),$$

$$\phi_{\text{NC}}^{\text{SNO}} = 5.21 \pm 0.27 (\text{stat}) \pm 0.38 (\text{syst}),$$

and the ratio of the ⁸B flux measured with the CC and NC reactions is

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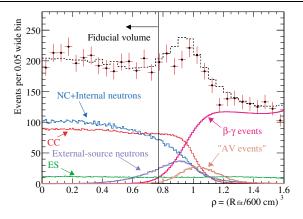


FIG. 3 (color). Volume-weighted radius (ρ) distribution (acrylic vessel = 1). Shown are the distributions for CC, ES, NC plus internal- and external-source neutrons, scaled from the fit, and separately determined external background distributions.

$$\frac{\phi_{\text{CC}}^{\text{SNO}}}{\phi_{\text{NC}}^{\text{SNO}}} = 0.306 \pm 0.026 \text{(stat)} \pm 0.024 \text{(syst)}.$$

Adding the constraint of an undistorted ⁸B energy spectrum to the analysis yields, for comparison with earlier results (in units of 10⁶ cm⁻² s⁻¹),

$$\phi_{\text{CC}}^{\text{SNO}} = 1.70 \pm 0.07(\text{stat})_{-0.10}^{+0.09}(\text{syst}),$$

$$\phi_{\text{ES}}^{\text{SNO}} = 2.13_{-0.28}^{+0.29}(\text{stat})_{-0.08}^{+0.15}(\text{syst}),$$

$$\phi_{\text{NC}}^{\text{SNO}} = 4.90 \pm 0.24(\text{stat})_{-0.29}^{+0.29}(\text{syst}),$$

consistent with the previous SNO measurements [2,3,16]. The difference between the CC results above (with and without constraint on the spectral shape) is $0.11 \pm 0.05(\text{stat})^{+0.06}_{-0.09}(\text{syst}) \times 10^6 \text{ cm}^{-2} \text{ s}^{-1}$.

The shape-unconstrained fluxes presented here combined with day and night energy spectra from the pure D₂O phase [12] place constraints on allowed neutrino flavor mixing parameters. Two-flavor active neutrino oscillation models predict the CC, NC, and ES rates in SNO [17]. New analysis elements included super-Kamiokande zenith spectra [18], updated Ga experiments [19,20], improved treatment of ⁸B spectral systematic uncertainties, and Cl and Ga cross section correlations [21]. This improved oscillation analysis applied to the pure D₂O data reproduces other results [21,22]. A combined χ^2 fit to SNO D2O and salt data alone yields the allowed regions in Δm^2 and $\tan^2\theta$ shown in Fig. 4. In a global analysis [23] of all solar neutrino data, the large mixing angle (LMA) region in Δ_m^2 and $\tan^2\theta$ is selected, as shown in Fig. 5(a). A global analysis including the KamLAND reactor antineutrino results [24] shrinks the allowed region further, with a best-fit point of $\Delta m^2 = 7.1^{+1.2}_{-0.6} \times 10^{-5} \text{ eV}^2$ and $\theta = 32.5^{+2.4}_{-2.3}$ degrees, where the errors reflect 1σ constraints on the two-dimensional region [Fig. 5(b)]. With the new SNO measurements the allowed

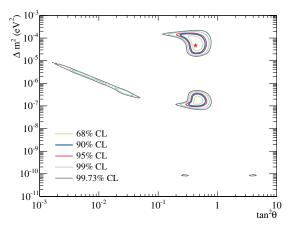


FIG. 4 (color). SNO-only neutrino oscillation contours, including pure D₂O day and night spectra, salt CC, NC, ES fluxes, with ⁸B flux free and *hep* flux fixed. The best-fit point is $\Delta m^2 = 4.7 \times 10^{-5}$, $\tan^2 \theta = 0.43$, $f_B = 1.03$, with $\chi^2/\text{DOF} = 26.2/34$.

LMA region is constrained to only the lower band at >99% C.L.. The best-fit point with one-dimensional projection of the uncertainties in the individual parameters (marginalized uncertainties) is $\Delta m^2 = 7.1^{+1.0}_{-0.3} \times 10^{-5} \text{ eV}^2$ and $\theta = 32.5^{+1.7}_{-1.6}$ degrees. This disfavors maximal mixing at a level equivalent to 5.4σ . In our analyses, the ratio f_B of the total ⁸B flux to the standard solar model [25] value was a free parameter, while the total hep flux was fixed at $9.3 \times 10^3 \text{ cm}^{-2} \text{ s}^{-1}$.

In summary, we have precisely measured the total flux of active 8B neutrinos from the Sun without assumptions about the energy dependence of the electron neutrino survival probability. The flux is in agreement with standard solar model calculations. These results combined with global solar and reactor neutrino results reject the hypothesis of maximal mixing at a confidence level equivalent to 5.4σ .

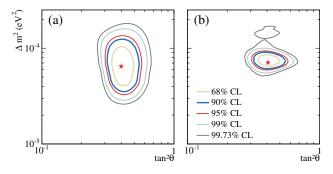


FIG. 5 (color). Global neutrino oscillation contours. (a) Solar global: D₂O day and night spectra, salt CC, NC, ES fluxes, Super-Kamiokande, Cl, Ga. The best-fit point is $\Delta m^2 = 6.5 \times 10^{-5}$, $\tan^2\theta = 0.40$, $f_B = 1.04$, with $\chi^2/\text{DOF} = 70.2/81$. (b) Solar global plus KamLAND. The best-fit point is $\Delta m^2 = 7.1 \times 10^{-5}$, $\tan^2\theta = 0.41$, $f_B = 1.02$. In both (a) and (b) the ⁸B flux is free and the *hep* flux is fixed.

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